

POLYTECHNIC UNIVERSITY
EL501: WIRELESS PERSONAL COMMUNICATIONS

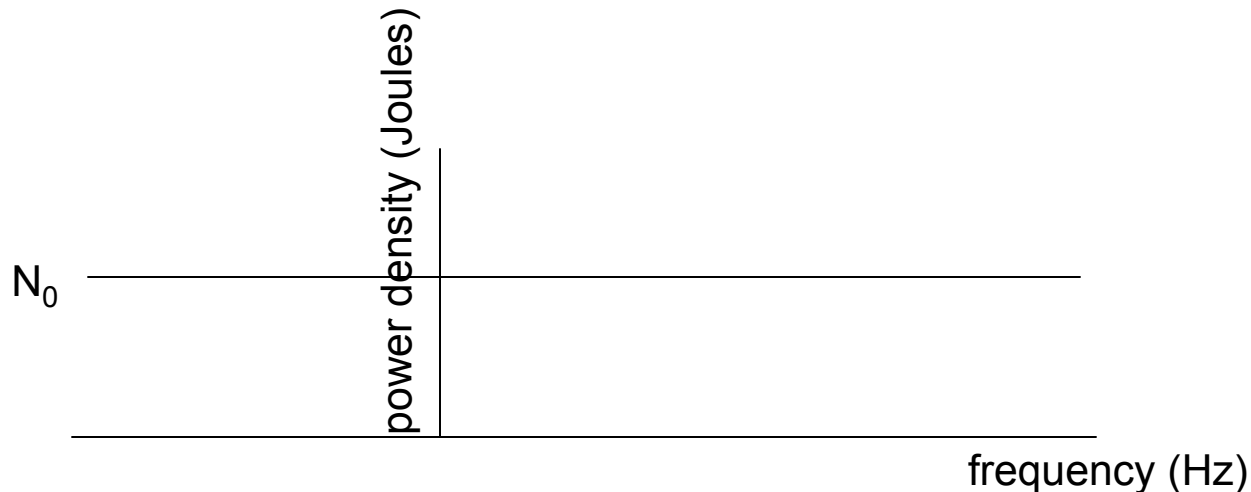
CAPACITY OF PRACTICAL CDMA SYSTEMS

Digital communication in white gaussian noise

ERROR RATE DEPENDS ON E_b/N_0

E_b JOULES IS THE ENERGY PER BIT

N_0 WATTS/Hz = N_0 JOULES IS THE POWER SPECTRAL DENSITY OF WHITE NOISE

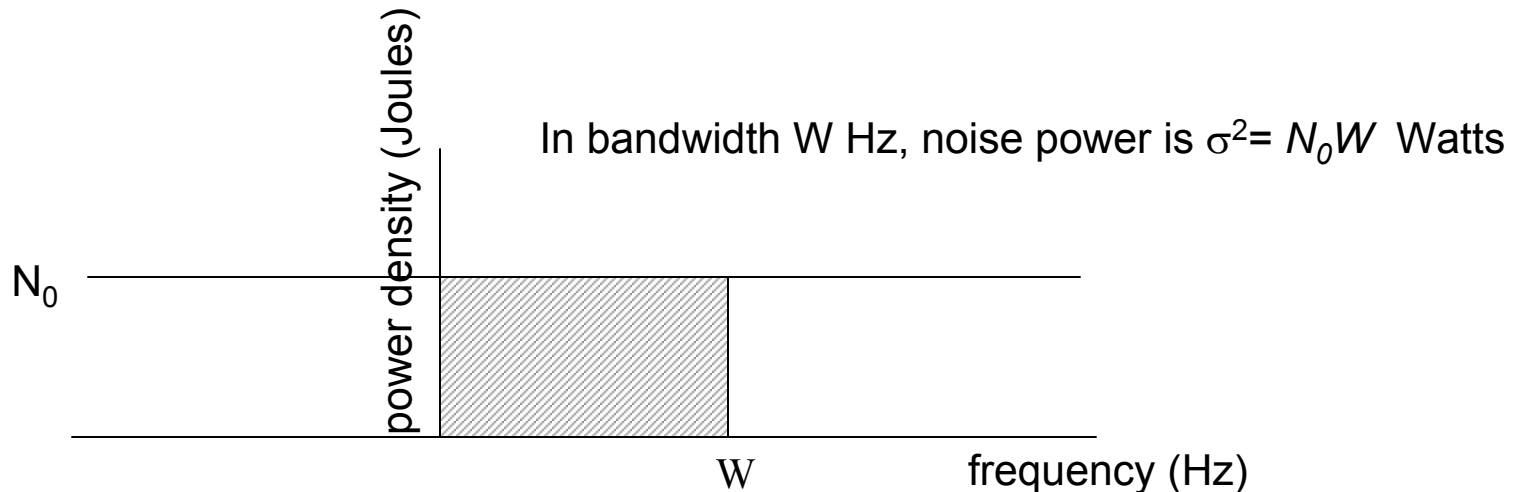


Digital communication in white gaussian noise

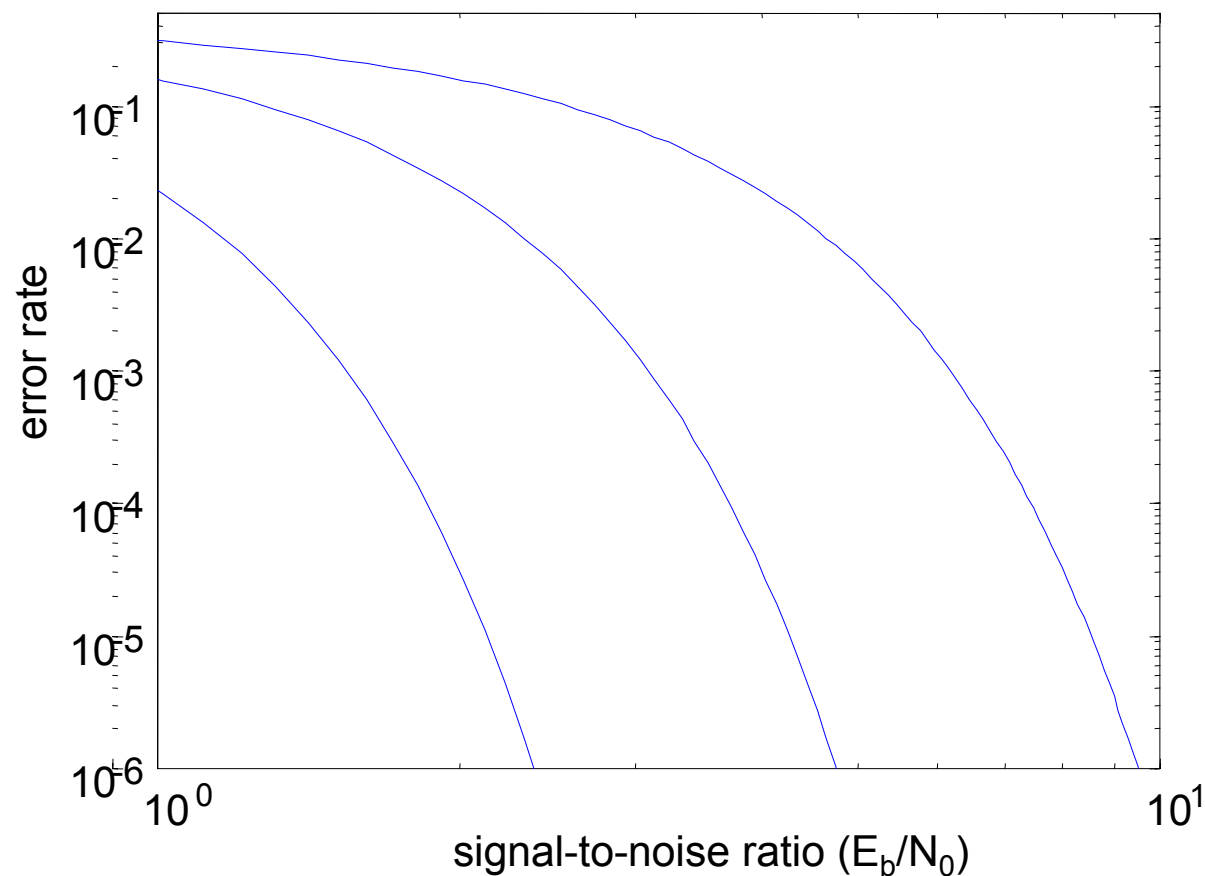
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Examples of error rate curves



SNR analysis

$$E_b = \int_0^T s^2(t) dt \quad \text{Joules}$$

If $s(t)$ is a constant envelope signal with received power level P_r Watts, bit rate = R b/s, bit duration = $T = 1/R$ seconds

$$E_b = P_r T = P_r / R \quad \text{Joules,}$$

$$\sigma^2 = N_0 W \quad \text{Watts}$$

$$N_0 = \sigma^2 / W \quad \text{Joules}$$

$$E_b / N_0 = \frac{W}{R} \frac{P_r}{\sigma^2}$$

Extend the analysis to CDMA

K SIMULTANEOUS TRANSMISSIONS

K-1 TRANSMISSIONS CAUSE INTERFERENCE *I Watts*

NOISE + INTERFERENCE POWER IS $\sigma^2 + I$ *Watts*

$$E_b / N_0 = \frac{W}{R} \frac{P_r}{\sigma^2 + I}$$

IF ALL *K* SIGNALS ARRIVE WITH POWER *P_r Watts*, THEN

$$I = (K-1)P_r \text{ *Watts*}$$

CDMA capacity

$$\begin{aligned} E_b / N_0 &= \frac{W}{R} \frac{P_r}{\sigma^2 + (K-1)P_r} \\ &= \frac{W}{R} \frac{1}{(K-1) + \sigma^2 / P_r} \end{aligned}$$

IF WE REQUIRE $E_b/N_0 \geq (E_b/N_0)_{req}$, THEN

$$K \leq \frac{W}{R} \frac{1}{(E_b / N_0)_{req}} + 1 - \frac{\sigma^2}{P_r}$$

CDMA capacity

$$K \leq \frac{W}{R} \frac{1}{(E_b / N_0)_{req}} + 1$$

INTERFERENCE LIMITED

$$\sigma^2 / P_r \approx 0$$

$$K \leq \frac{W}{R} \frac{1}{(E_b / N_0)_{req}}$$

NOISE POWER & SIGNAL POWER
APPROXIMATELY THE SAME

$$\sigma^2 \approx P_r$$

$$K \leq \frac{G}{(E_b / N_0)_{req}}$$

MODEM HAS 1 b/s/Hz, THEN

$W = R_c$ CHIPS PER SECOND

$W/R = R_c/R = G$, PROCESSING GAIN

Other properties of practical CDMA systems

- speech activity detection increase by F_{speech}
- directional antennas increase by $F_{sectors}$
- interference from other cells decrease by F_{cells}
- unequal received signal powers decrease by F_{power}

$$C = \frac{W}{R} \frac{1}{(E_b / N_0)_{req}} \frac{F_{sectors} F_{speech}}{F_{power} F_{cells}}$$

IS-95 CDMA

- $W/R = 1.2288/9600 = 128$
- $4 \text{ (6 dB)} < E_b/N_0 < 5 \text{ (7 dB)}$
- $2 < F_{\text{speech}} < 3$
- $F_{\text{sectors}} \approx 2.4$
- $F_{\text{cells}} \approx 1.6$
- $1.05 < F_{\text{power}} < 3.3$

23 < conversations/base station < 137