

POLYTECHNIC UNIVERSITY  
EL501: WIRELESS PERSONAL COMMUNICATIONS

INTRODUCTION TO  
SPREAD SPECTRUM  
COMMUNICATIONS

# WIRELESS COMMUNICATIONS SIGNALS

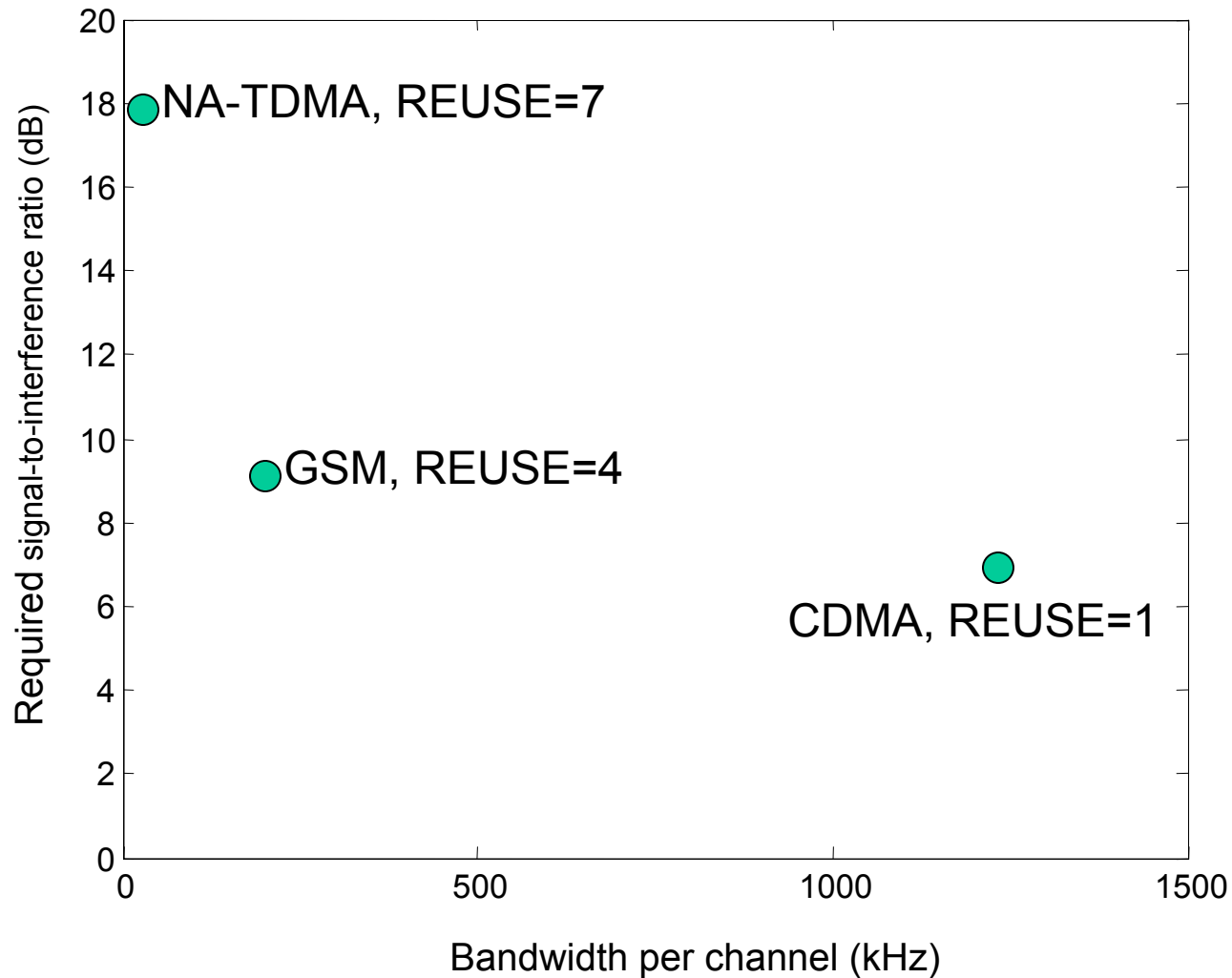
- IMPORTANT PROPERTIES ARE:
  - BANDWIDTH,  $W$  (Hz)
  - IMMUNITY TO INTERFERENCE  $10\log(\gamma_{\text{req}})$  (dB)
- IN CELLULAR, IMMUNITY TO INTERFERENCE AND BANDWIDTH TOGETHER DETERMINE EFFICIENCY
  - AMPS, NA-TDMA:  $W=30$  kHz  $\gamma_{\text{req}}=18$  dB
  - GSM  $W=200$  kHz  $\gamma_{\text{req}}=9$  dB

# SPREAD SPECTRUM SIGNALS

- SPREAD SPECTRUM SYSTEMS HAVE HIGH  $W$  AND LOW  $\gamma_{\text{req}}$

– CDMA:  $W=1.25$  MHz  $\gamma_{\text{req}}=7$  dB

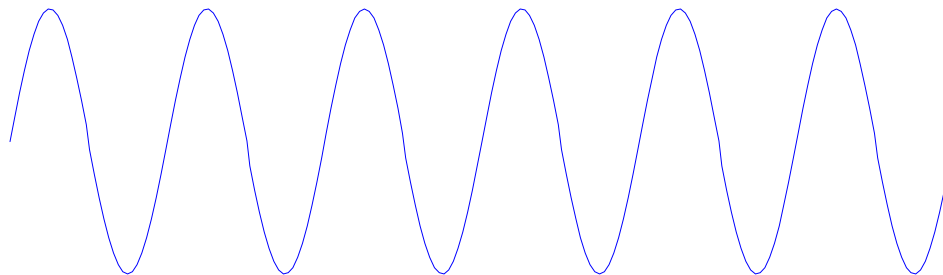
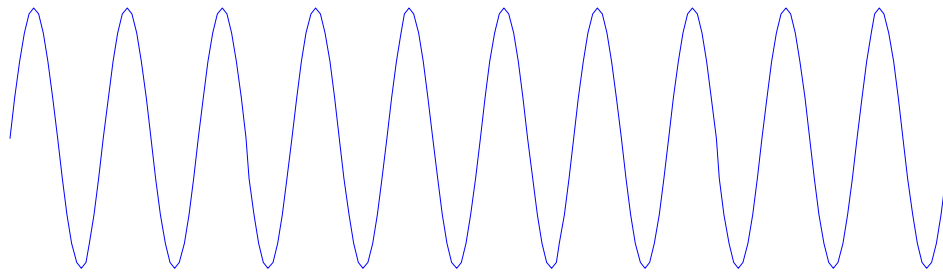
# BANDWIDTH AND IMMUNITY TO INTERFERENCE



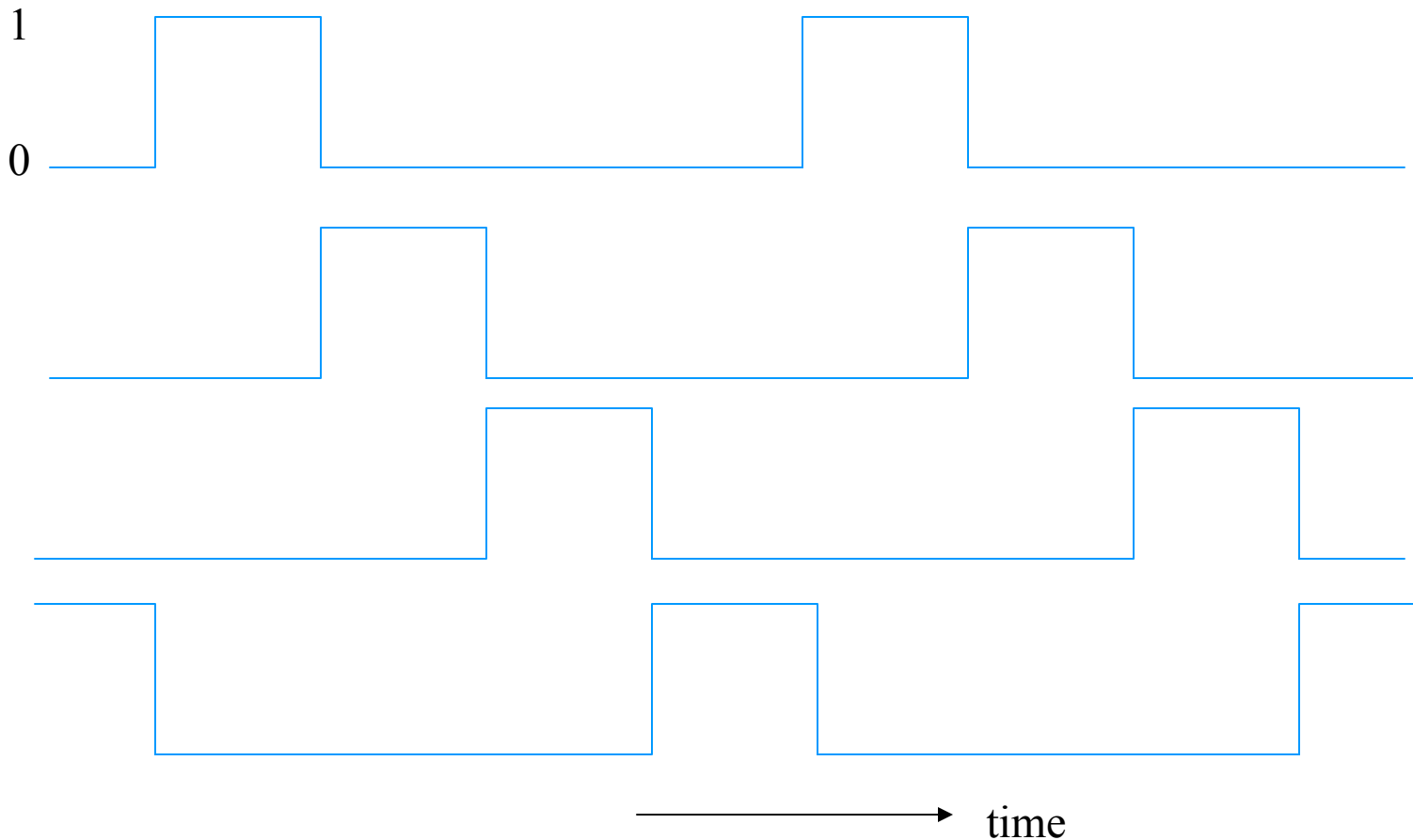
# MULTIPLE ACCESS/MULTIPLEX & MODULATION

- MULTIPLE ACCESS/MULTIPLEXING: EACH COMMUNICATION HAS ITS OWN **CARRIER**
  - CARRIERS CAN BE ORTHOGONAL OR NOT
- MODULATION: MODIFY A CARRIER ACCORDING TO THE INFORMATION TO BE SENT

# SINE WAVE CARRIERS (FREQUENCY DIVISION)

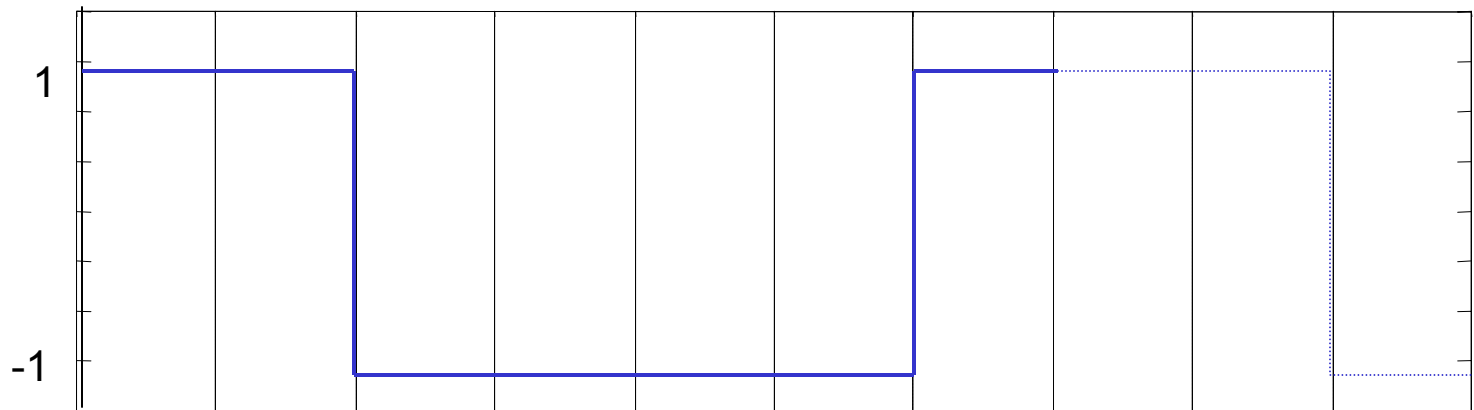
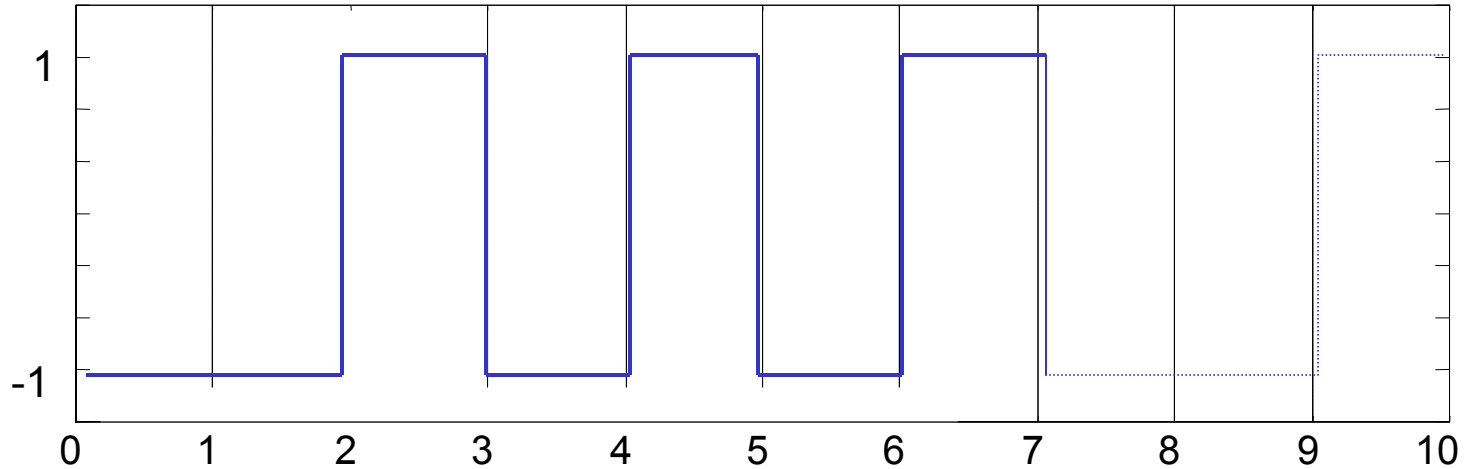


# ON-OFF CARRIERS (TIME DIVISION)



# DIRECT SEQUENCE CARRIERS (7 CHIPS)

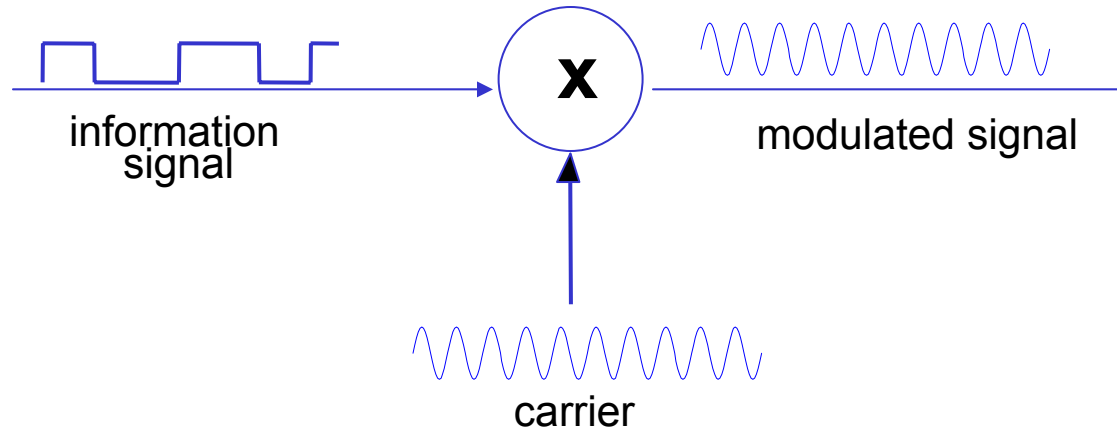
**CARRIER 1 = -1 -1 1 -1 1 -1 1**



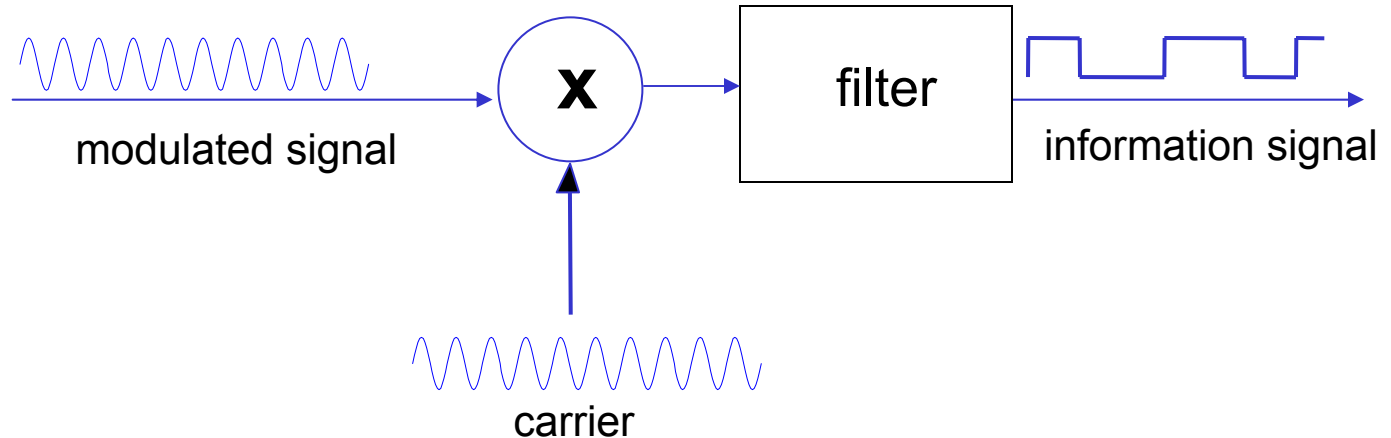
**CARRIER 2 = 1 1 -1 -1 -1 -1 1**

# MODULATION & DEMODULATION

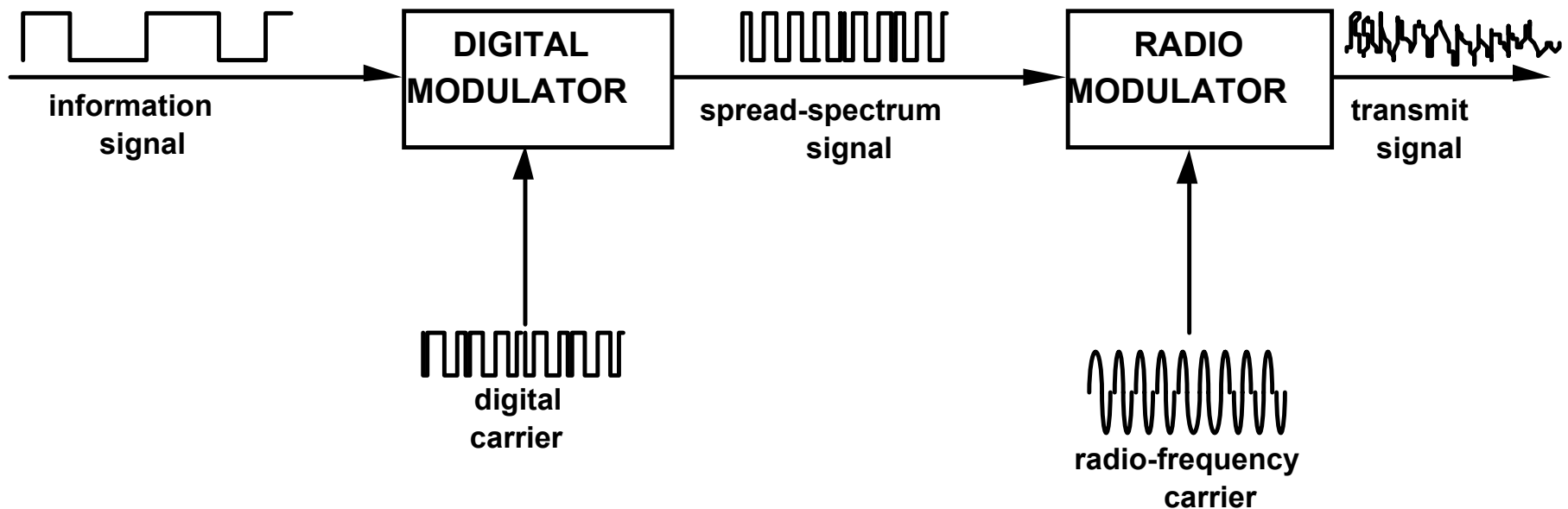
MO



DEM



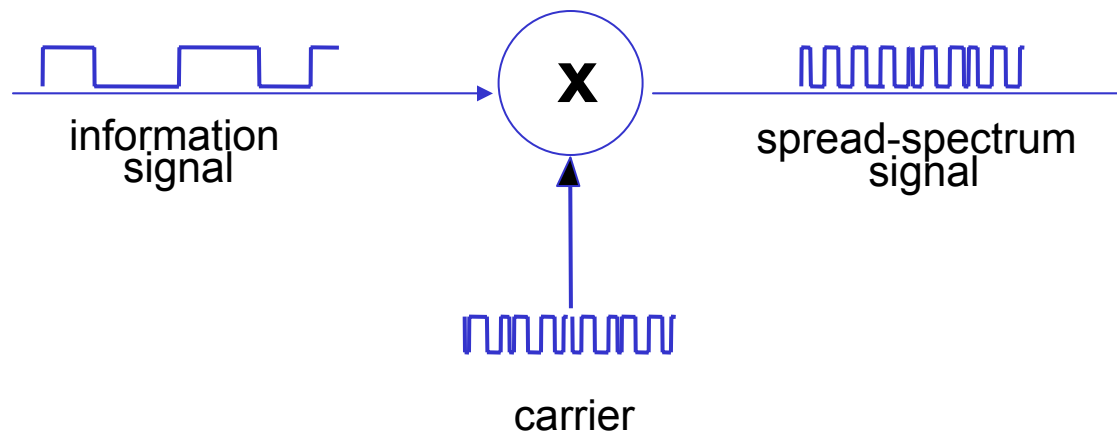
# DIGITAL MODULATOR & RADIO MODULATOR



MODULATION AND  
MULTIPLE ACCESS

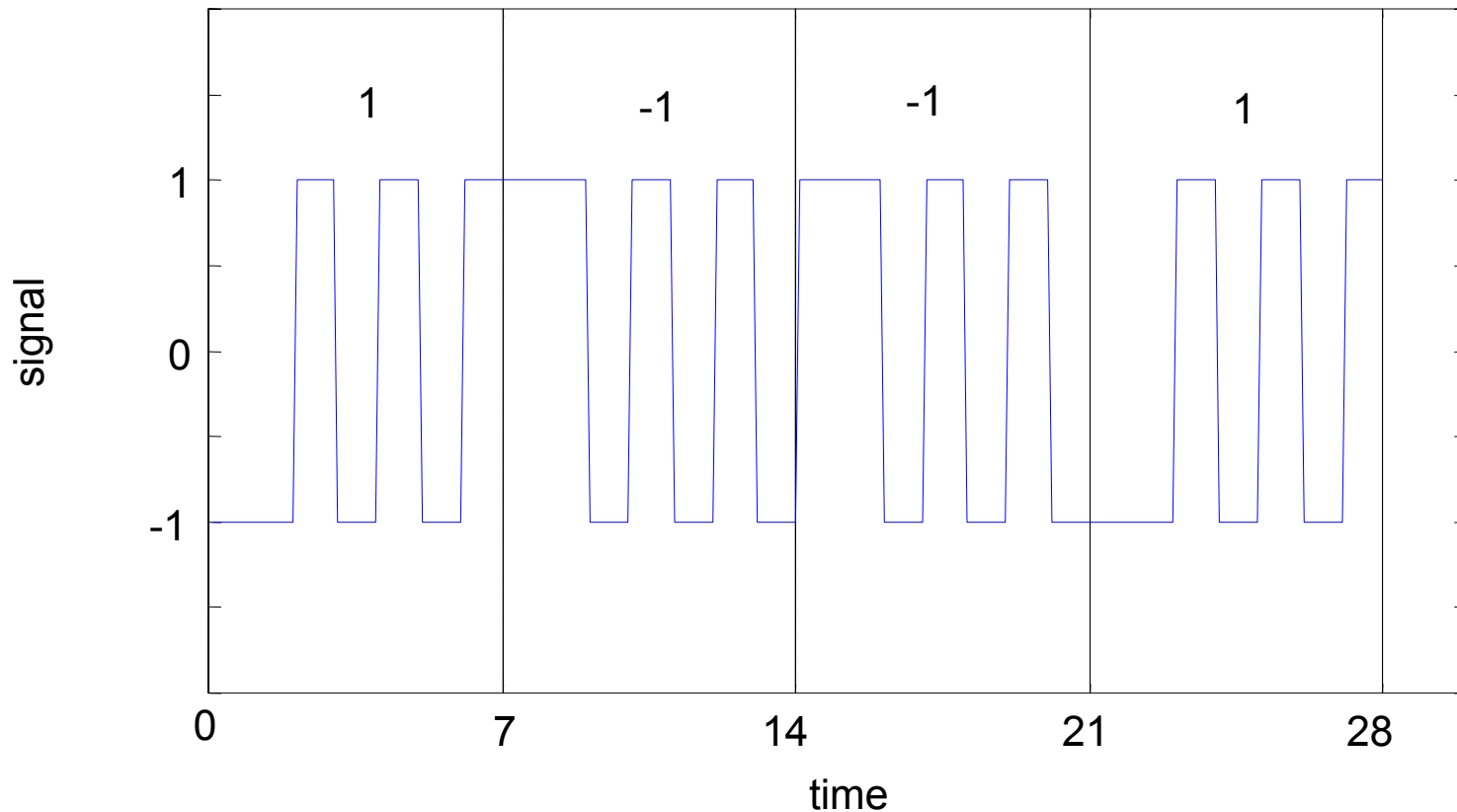
MODULATION AND  
FREQUENCY TRANSLATION

# SPREAD SPECTRUM MODULATION



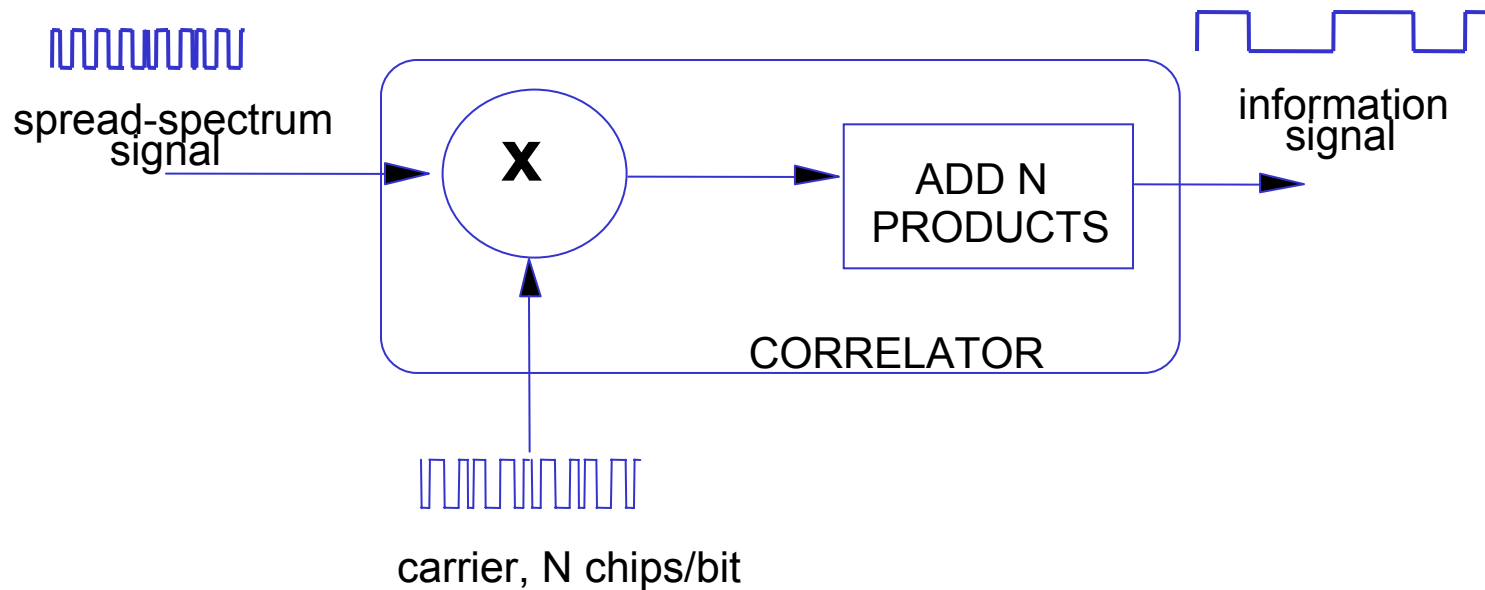
# TRANSMIT 4 BITS

CARRIER 1 X [1 -1 -1 1]



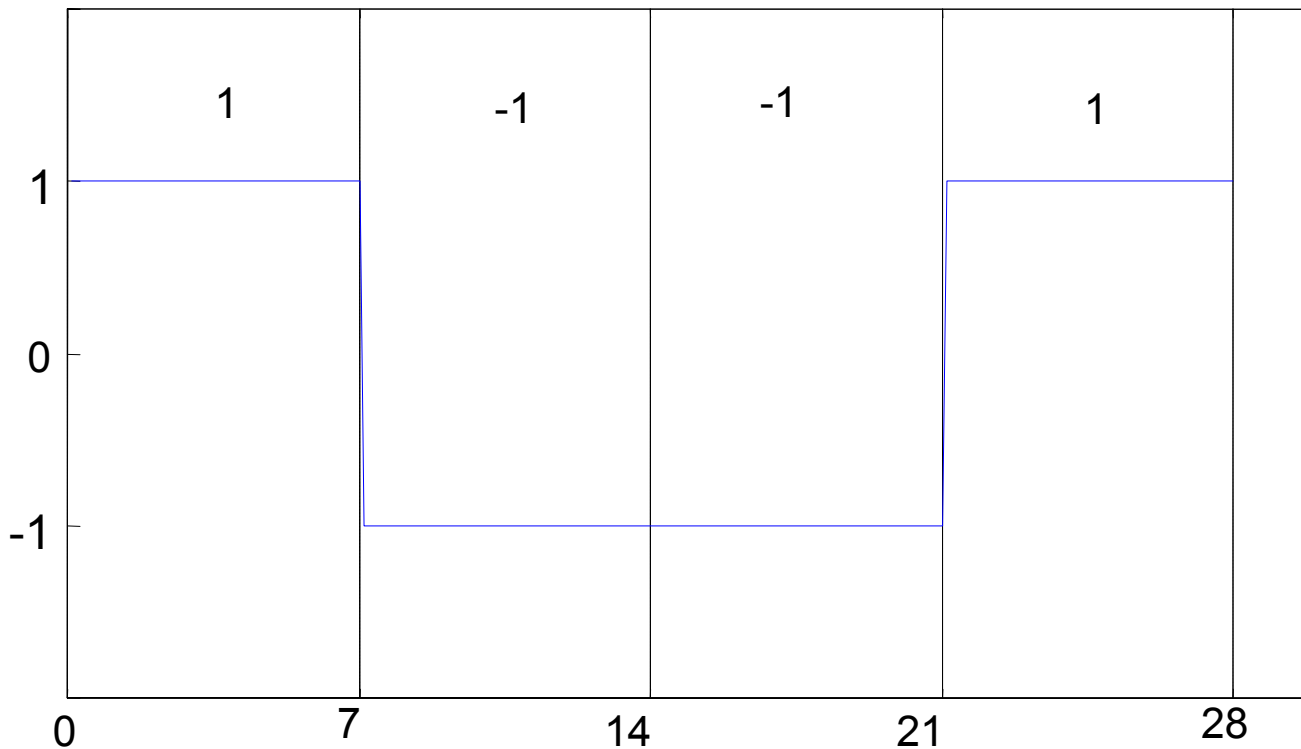
# DEMODULATION

## DIGITAL MATCHED FILTER

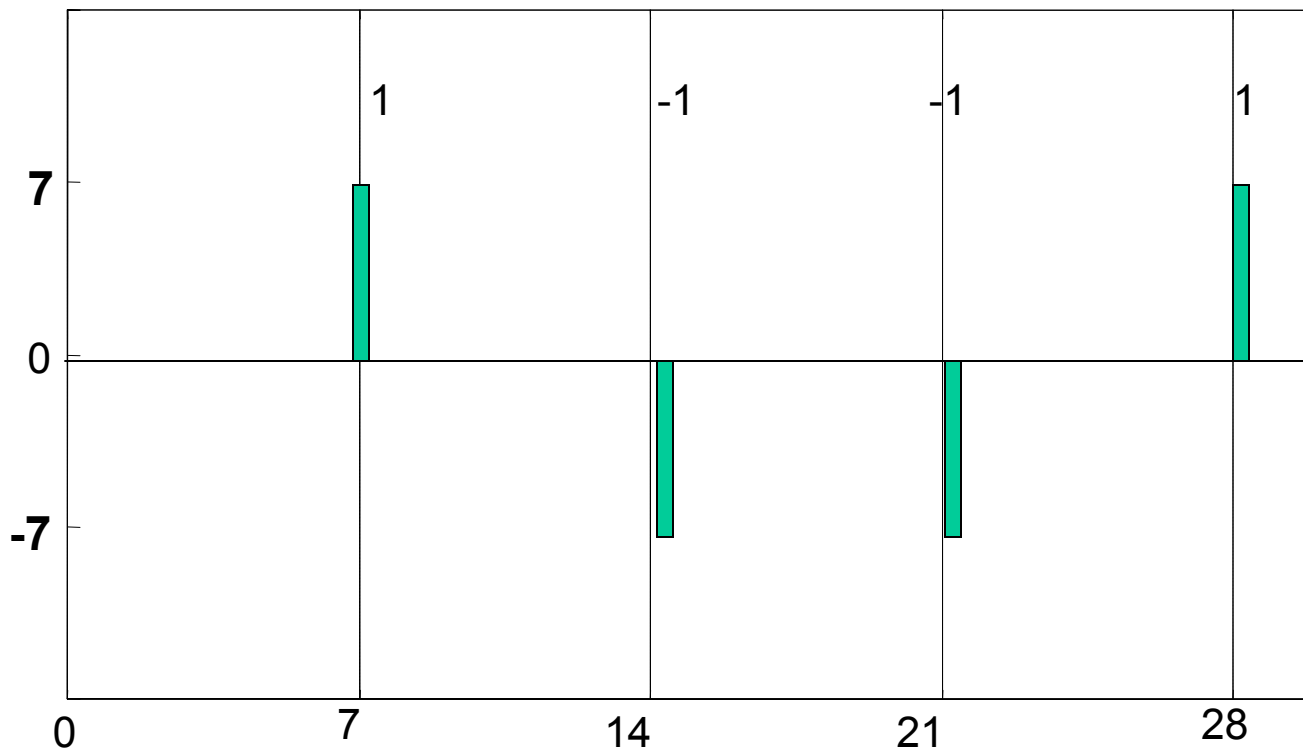


# MULTIPLIER OUTPUT

(CARRIER 1 X SS SIGNAL)

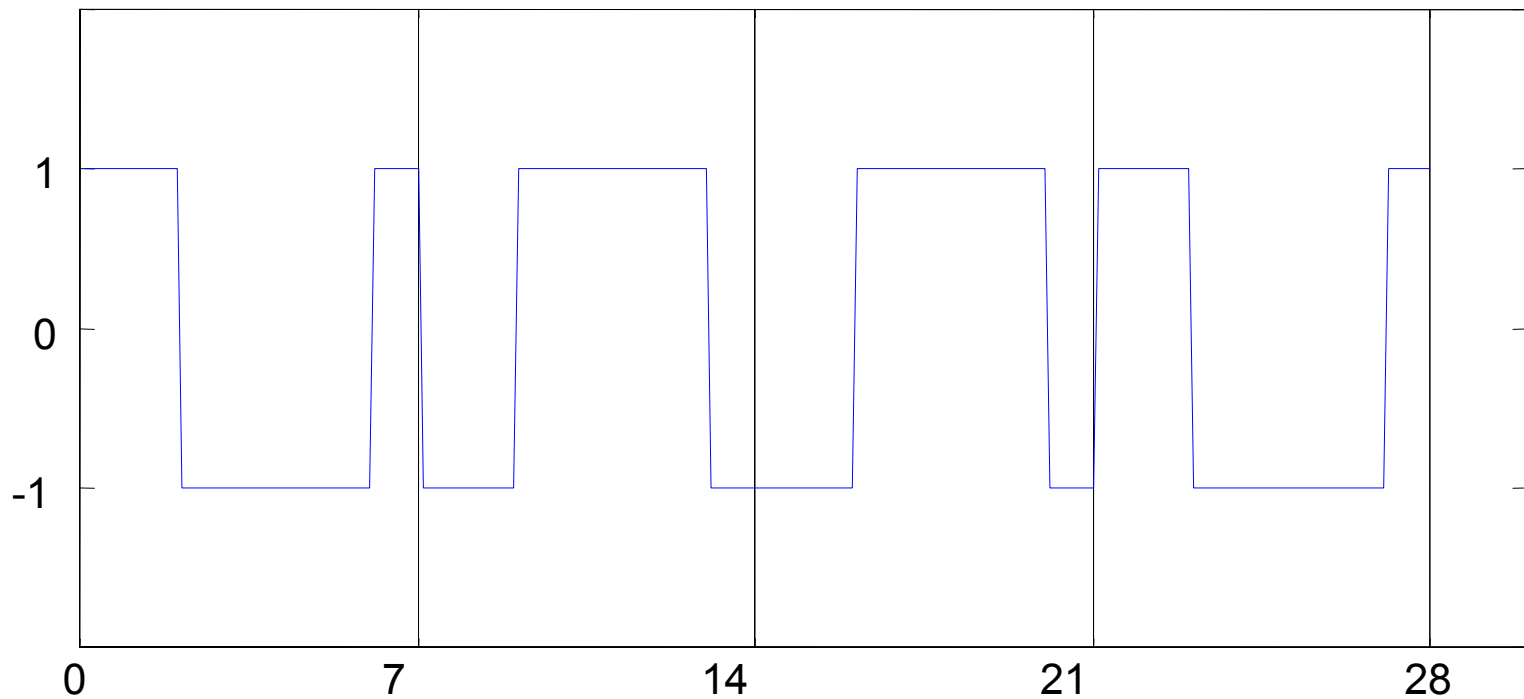


# CORRELATOR OUTPUT AFTER ADDING 7 PRODUCTS (PROCESSING GAIN = 7)

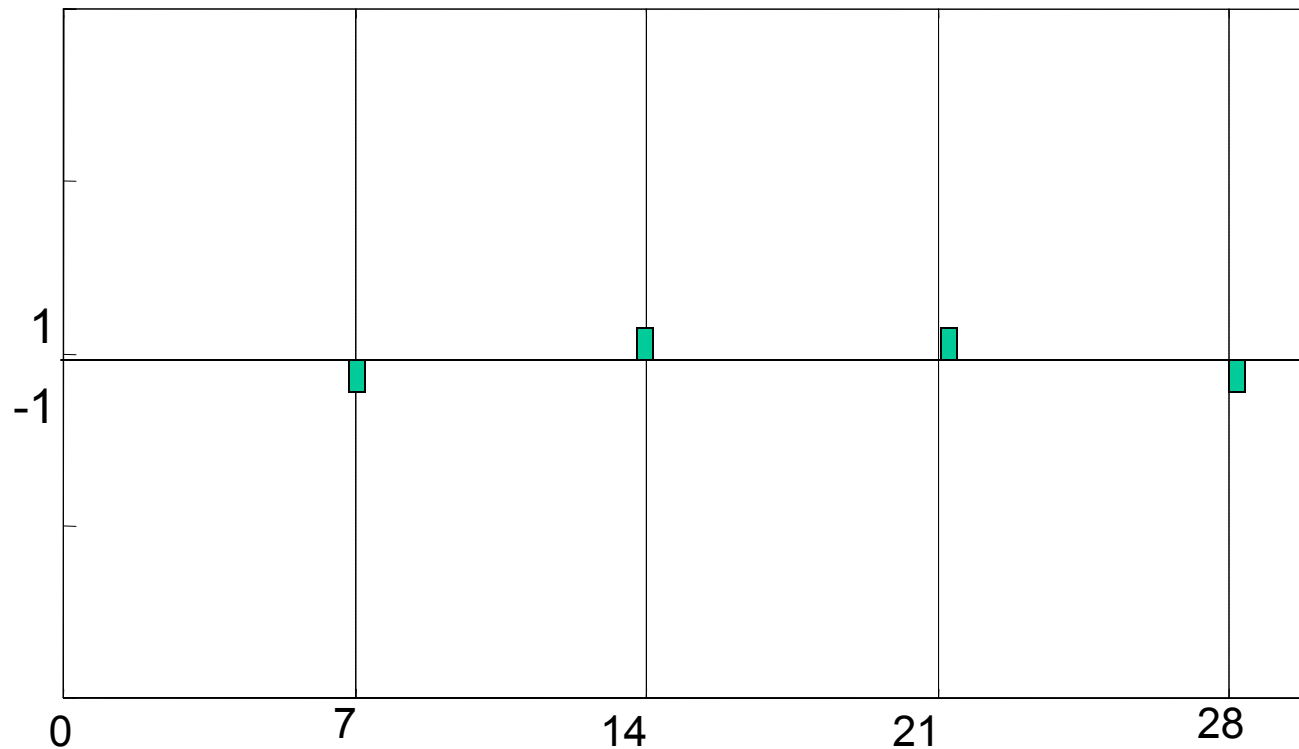


# MULTIPLY SS SIGNAL BY CARRIER 2

(INTERFERENCE IN A DIFFERENT RECEIVER)



# CORRELATOR OUTPUT IN SECOND RECEIVER



# Probability of error

- Reference user has a code with  $G$  chips, all  $+1$ .
- Transmitted bit is  $+1$
- At the receiver the reference user contributes  $G$  to the correlator output
- Other users have codes  $G$  chips each is  $+1$  or  $-1$  selected randomly
- Interfering users transmit  $+1$  or  $-1$  at random

# Probability of error

- At the receiver each interfering user contributes the sum of  $G$  random variables to the correlator output.
- Each random variable  $x$  is  $+1$  or  $-1$  with probability  $\frac{1}{2}$ .
- $E[X]=0$ ;  $\text{var}[X]=1$
- With  $K-1$  interfering users, the interference is the sum of  $G(K-1)$  independent identically distributed random variables.

# Probability of error

- The expected value of the sum of  $G(K-1)$  iid random variables, each with  $E[X] = 0$ , is  $G(K-1)E[X]=0$
- The variance of the sum of  $G(K-1)$  iid random variables, each with  $\text{Var}[X] = 1$ , is  $G(K-1)\text{Var}[X]=G(K-1)$
- An error (-1 received) occurs when the signal + interference  $< 0$ .
- Because the signal part of the output is  $G$ , an error occurs when interference  $< -G$ .

# Probability of error

- The interference  $I$  is a random variable with
  - $E[I]=0$  and  $\text{Var}[I]=G(K-1)$ .

- The probability of error  $P_e$  is the probability  $I < -G$ :

$$P_e = \int_{-\infty}^{-G} f_I(x) dx$$

- $I$  is related to a binomial random variable and it is not hard to write the formula for its probability density (actually it is a probability mass function).

# Probability of error

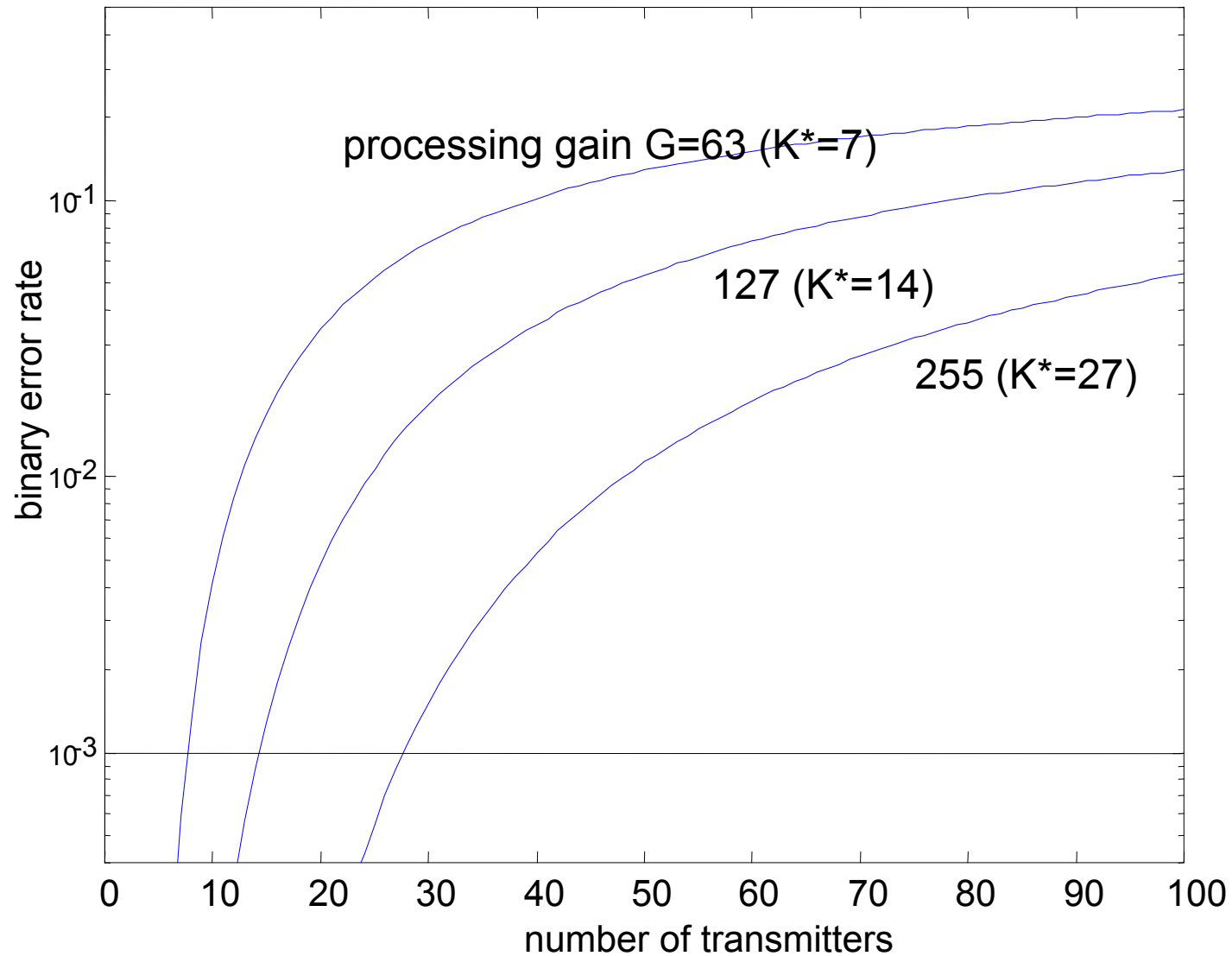
- However, it is more convenient to use the Gaussian approximation to  $f_I(x)$ :

$$f_I(x) = \frac{1}{\sqrt{2\pi\text{Var}[I]}} \exp\left(-\frac{(x - E[I])^2}{2\text{Var}[I]}\right)$$

- With this approximation

$$P_e = \int_{-\infty}^{-G} f_I(x) dx = \frac{1}{\sqrt{2\pi}} \int_{\sqrt{\frac{G}{K-1}}}^{\infty} \exp\left(-\frac{u^2}{2}\right) du = Q\left(\sqrt{\frac{G}{K-1}}\right)$$

# Soft capacity



# Additional considerations in practical systems

- Signals from different terminals do not arrive in synchronism at base station
- Signals from different terminals arrive with different strength at base station
- Error correcting and error detecting codes
- Channel conditions: interference from other cells, fading, multipath, etc.

**Use “top down” approach to estimate capacity**